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Consequences of Urban Stability Conditions for Computational Fluid Dynamics

Simulations of Urban Dispersion

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Abstract.

The validity of omitting stability considerations when simulating transport and dispersion in the urban environment is explored using observations from the Joint URBAN 2003 field experiment and computational fluid dynamics simulations of that experiment. Four releases of sulfur hexafluoride, during two daytime and two nighttime intensive observing periods, are simulated using the building-resolving computational fluid dynamics model, FEM3MP to solve the Reynolds Averaged Navier-Stokes equations with two options of turbulence parameterizations. One option omits stability effects but has a superior turbulence parameterization using a non-linear eddy viscosity (NEV) approach, while the other considers buoyancy effects with a simple linear eddy viscosity (LEV) approach for turbulence parameterization. Model performance metrics are calculated by comparison with observed winds and tracer data in the downtown area, and with observed winds and turbulence kinetic energy (TKE) profiles at a location immediately downwind of the central business district (CBD) in the area we label as the urban shadow. Model predictions of winds, concentrations, profiles of wind speed, wind direction, and friction velocity are generally consistent with and compare reasonably well with the field observations. Simulations using the NEV turbulence parameterization generally exhibit better agreement with observations.

To further explore this assumption of a neutrally-stable atmosphere within the urban area, TKE budget profiles slightly downwind of the urban wake region in the “urban shadow” are examined. Dissipation and shear production are the largest terms which may be calculated directly. The advection of TKE is calculated as a residual; as would be expected downwind of an urban area, the advection of TKE produced within the urban area is a very large term. Buoyancy effects may be neglected in favor of advection, shear production, and dissipation. For three of the IOPs, buoyancy production may be neglected entirely, and for one IOP, buoyancy production
contributes approximately 25% of the total TKE at this location. For both nighttime releases, the contribution of buoyancy to the total TKE budget is always negligible though positive.

Results from the simulations provide estimates of the average TKE values in the upwind, downtown, downtown shadow, and urban wake zones of the computational domain. These values suggest that building-induced turbulence can cause the average turbulence intensity in the urban area to increase by as much as seven times average “upwind” values, explaining the minimal role of buoyant forcing in the downtown region. The downtown shadow exhibits an exponential decay in average TKE, while the distant downwind wake region approaches the average upwind values. For long-duration releases in downtown and downtown shadow areas, the assumption of neutral stability is valid because building-induced turbulence dominates the budget. However, further downwind in the urban wake region, which we find to be approximately 1500 m beyond the perimeter of downtown Oklahoma City, the levels of building-induced turbulence greatly subside, and therefore the assumption of neutral stability is less valid.
1. Introduction

Due to large populations and difficult evacuation logistics, urban areas are the most consequential locations for an atmospheric release of hazardous material, whether the release is due to an industrial accident or to an act of terrorism. To protect urban populations, the use of observational and/or modeling tools is necessary in order to track and forecast the transport and dispersion of the hazardous material from such releases. The need for robust modeling tools was stressed in a recent report by the National Research Council of the National Academies (2003). Specifically, the report states that two categories of models are needed: (1) advanced rapid-execution models for emergency response applications, and (2) slower but more accurate computational fluid dynamics (CFD) models for situations such as emergency preparedness and post-event analyses.

Several CFD models are available and are continually being tested with data from actual releases of tracer material in urban areas such as Salt Lake City (e.g., Chan and Leach (2004)), Oklahoma City, and New York City. These releases have taken place at various times of day and in all seasons. Yet many modeling tools often assume that nearly neutral conditions are appropriate to use for the entire urban area being simulated, perhaps due to the lack of representative field measurements or sufficiently sophisticated turbulence models. A strong argument supports the application of neutral stability to urban environments: atmospheric stability (as defined by the Richardson number) is determined by both mechanical stresses and buoyant forcing. For an urban setting, building-induced mechanical stresses are thought to dominate the production of turbulence, overriding any stability effects and creating nearly neutral atmospheric conditions at least in the most densely-built-up urban areas and immediately downwind of these areas.
Results from our recent simulations of two releases of sulfur hexafluoride gas in the Oklahoma City urban area using a CFD model - FEM3MP – appear to support partially the assumption that urban areas tend toward neutral stability. Based on a model-data comparison for winds and concentration in the near field and velocity and turbulence profiles in the urban wake region, Chan and Leach (2007) observed that the neutral stability assumption appears to be valid for intensive operation period (IOP) 9 (a nighttime release with moderate winds) and also appears to be valid for IOP 3 (a daytime release with strong buoyant forcing) in the urban core area but is less valid in the urban wake region.

In this study, a more definitive characterization of stability conditions associated with the simulated releases is presented. We document the neutral stability caused by the enhancement of mechanical mixing in the urban core region and the decay of that enhanced turbulence downwind. We first describe our CFD model and the field experiments simulated. We present results from a model-data comparison for both the wind and concentration fields from four releases, using two different turbulence parameterizations, one considering buoyancy effects with a simple linear eddy viscosity (LEV) approach for modeling mechanical production of turbulence and one omitting stability effects but with a superior non-linear eddy viscosity (NEV) approach for modeling turbulence processes. We next examine observed TKE budgets from a profile located immediately downwind of the urban area, with special attention to the role of observed buoyant forcing relative to the total TKE in the urban wake. Finally, we compare the predicted TKE fields within the central business district urban zone to upwind and downwind zones in order to delineate the regions in which urban-generated turbulence dominates other means of turbulence production.
2. The CFD model

Our model, developed under the sponsorship of the U.S. Department of Energy (DOE) and Department of Homeland Security (DHS), is based on solving the three-dimensional, time-dependent, incompressible Navier-Stokes equations on massively parallel computer platforms. The numerical algorithm is based on finite-element discretization for effective treatment of complex building geometries and variable terrain, together with a semi-implicit projection scheme and modern iterative solvers developed by Gresho and Chan (1998) for efficient time integration. Physical processes treated in our code include turbulence modeling via Reynolds Averaged Navier-Stokes (RANS) and Large Eddy Simulation (LES) approaches (Calhoun et al., 2005), atmospheric stability, aerosols, UV radiation decay, surface energy budgets, and vegetative canopies, etc. For convenience of code parallelization and computational speed, our current version of FEM3MP employs a structured mesh (but graded and distorted mesh is allowed) and explicitly-resolved buildings within the computational domain are represented as solid blocks with velocity, pressure, and diffusivities set equal to 0.

While high-resolution CFD models are very useful for emergency planning, vulnerability analyses, and post-event analyses, such models usually require excessive computer resources and long turnaround times, thus rendering them unwieldy. As a means to improve the efficiency of FEM3MP, a simplified CFD approach, in which only targeted and important buildings are explicitly resolved using fine grid resolution and the remaining buildings are represented as drag forces (virtual buildings) using much coarser grid resolution, was implemented and demonstrated by Chan et al. (2004). The virtual building approach is discussed in detail in Chan and Leach (2007).
The present simulations resolve certain buildings with fine grid resolution and treat the remaining buildings as drag elements (virtual buildings) with coarser grid resolution. Buildings in the near-field, within five hundred meters of tracer releases, and buildings taller than 40m are typically defined explicitly. Because the mixed explicit-virtual building approach reduces the number of grid points by approximately a factor of ten (depending on the user’s choice of which buildings to make virtual), computational savings are also approximately an order of magnitude. However, the solution in the vicinity of virtual buildings is slightly less accurate because of coarser grid resolution and the presence of small values of velocity and diffusivities at the grid points associated with virtual buildings.

Turbulence within FEM3MP is typically parameterized with the nonlinear eddy viscosity (NEV) turbulence parameterization, which solves three turbulence equations as discussed in Gresho and Chan (1988). However, one limitation of our present version of the NEV turbulence model is that it assumes that the atmosphere being simulated is neutrally-stable, that neither strong convection nor strong stratification is present. The present study seeks to determine the impact of such assumption on the ability of FEM3MP to simulate the continuous releases of SF$_6$ during Joint URBAN 2003 IOPs 2, 3, 8, and 9. For comparison, simulations utilizing a simpler (LEV) turbulence parameterization are also considered. The LEV parameterization (Chan et al., 1987, Calhoun et al., 2004) does consider the effects of atmospheric stability via a Monin-Obukhov-based stability function, but it is based on K-theory for turbulence parameterization and is therefore less sophisticated than the NEV parameterization.

3. The Joint Urban 2003 field study

To provide quality-assured, high-resolution meteorological and tracer data sets for evaluation and validation of indoor and outdoor urban dispersion models, the U.S. DHS and DoD – Defense
Threat Reduction Agency co-sponsored a series of dispersion experiments, named Joint URBAN 2003, in Oklahoma City (OKC), Oklahoma, during July 2003 (Allwine, et al., 2004). These experiments took place during daytime and nighttime to include both convective and stable atmospheric conditions. A total of ten IOPs were conducted and SF$_6$ in the form of puffs or continuous sources were released over 6 daytime and 4 nighttime episodes.

Many wind and concentration sensors were used to collect wind and SF$_6$ data over both long (up to 30 minutes) and short (0.1 sec) time-averaging periods. In addition to measurements near the surface, wind and concentration profiles adjacent to the outside walls of several buildings were also taken. In one nocturnal case, balloons were deployed close to the tracer release area. Many of the released balloons exhibited quick ascents from ground level to the top of buildings, implying localized convection. For the present study, model predictions of SF$_6$ concentrations are compared with 15-minute averages taken from “Blue Boxes”, which collected 10 20-cc “sips” of air into a 200-cc bag over 15-minute intervals from an intake valve about 1.5m above the ground surface. The air samples from each bag were then analyzed using a Hewlett-Packard 5890 Series II gas chromatograph (GC) equipped with a model G1223A electron capture detector (ECD). The GC was calibrated using 49 sulfur hexafluoride standards ranging in concentration from 9.3 part per trillion (ppt) to 980 part per billion (ppb). Five separate contiguous calibration curves were constructed to quantify samples throughout the entire range. Extrapolation of the low level calibration curve with intercept forced through the origin was used to quantify samples below 9.3 ppt. Samples above 980 ppb were diluted to provide SF$_6$ concentrations within the calibration range. A set of 14 calibration check standards was used to monitor system stability and selected samples were run in replicate.
Many of the in situ meteorological observations during JU2003 were within the urban canopy layer, at or below the mean height of the buildings in the immediate vicinity of the observations. Particularly useful for comparison with CFD predictions in the urban area are the Dugway Proving Ground (DPG) PWIDS wind observations, collected by anemometers mounted on streetlights.

Measurements immediately downwind of the central business district (CBD) were obtained using a pseudo-tower (a ladder under tension, anchored by a construction crane) located about 750 m north of downtown OKC. At eight levels (7.8 m, 14.6 m, 21.5 m, 28.3 m, 42.5 m, 55.8 m, 69.7 m, and 83.2 m) along this crane, R.M. Young Model 81000 ultrasonic anemometers were mounted, providing wind speed, wind direction, and virtual temperature measurements at those levels. The highest observation level was well above the mean building height of the Oklahoma City CBD (approximately 35 m) but below the height of the two tallest single buildings (approximately 120 m). Details on the construction of this pseudo-tower are presented in Gouveia et al. (2007). Virtual temperature profiles from this platform are not suitable for estimating atmospheric stability.

Each 30-minute time series of 10 Hz data from the crane sonic anemometers is processed in the following fashion. First, to correct for any tilting in the sonic anemometer as mounted, the planar-fit tilt correction algorithm (Wilczak et al., 2001) is applied to the data; each 30-minute time series is corrected independently. After the tilt correction is applied, the mean wind direction over the 30-minute segment is calculated. In the event that the wind direction is north-westerly to north-easterly (315 to 360 degrees or 0 to 45 degrees), the data are rejected from further inspection due to expected contamination by the supporting crane. Northerly winds did not occur during any of the IOPs discussed here. The horizontal velocity data are rotated into a
right-handed natural coordinate system, so that the streamwise coordinate $u$ is aligned with the mean wind, the transverse component $v$ is perpendicular to $u$ in the horizontal plane. $w$ remains perpendicular to $u$ in the vertical plane. For momentum and heat flux calculations, the mean of each time series over 30-minutes is removed. Measurements of turbulent kinetic energy (TKE) dissipation rate are also obtained from these data, using the inertial estimation method as described in Piper and Lundquist (2004).

Most terms of the TKE budget can be calculated from the crane dataset. The TKE budget is written

$$\frac{\partial e}{\partial t} + U_i \frac{\partial e}{\partial x_j} = \delta_{ij} \frac{g}{\theta_v} \left( u_i' \theta_v' \right) - u_i' u_j \frac{\partial U_i}{\partial x_j} - \frac{\partial u_j'}{\partial x_j} \epsilon - \frac{1}{\rho} \frac{\partial u_j'}{\partial x_j} - \epsilon$$

as in Stull (1988), or

$$T + A = B + S + TT + P - D,$$

where $T$ represents the local storage or tendency of TKE, $A$ represents the advection of TKE, $B$ represents buoyant production or destruction of TKE, $S$ represents shear production of TKE, $TT$ represents the turbulent transport of TKE, $P$ represents the pressure transport term, and $D$ represents the dissipation rate of TKE. From the profile of sonic anemometers at the crane, $D$, $TT$, $S$, and $B$ may be calculated, either uniquely from observations at each level, as for dissipation and buoyant production, or from spline fits to the profile of measurements, as for turbulent transport and shear production. The local storage or tendency term may also be estimated from the change in TKE at each level from one time series to the next time series; for the IOPs studied here, the storage term calculated in that fashion is one to two orders of magnitude smaller than $S$, the shear production term. The estimation of the pressure transport term would require sensitive pressure fluctuation instrumentation, and this term would include the transport or destruction of TKE by wave motions. The advection term, $A$, is expected to be the largest term at a location in
an urban shadow. Without similar observations upwind and downwind of the crane, this advection term must be calculated as a residual, which lessens the confidence in this estimate as it now includes all errors from the calculations of the other terms, as well as any influence from pressure transport $P$.

To estimate the contribution of buoyant forcing to the total amount of TKE observed, the rate of buoyant production of TKE ($B$) is multiplied by a turbulent time scale $\tau$, which is determined from the quotient of mean observed TKE over mean observed dissipation rate, following the model of Zeierman and Wolfshtein (1986). As discussed below, observed values of this time scale range from 60 to 170 seconds for these IOPs. This turbulent time scale is smaller than a typical convective turbulence time scale (approximated by the quotient of boundary-layer height $h$ over a convective velocity $w^*$) of 600 seconds. Shorter turbulent time scales are expected in an urban boundary layer given the local circulations (both thermal and mechanical) generated in such an environment.

4. Model-data comparison

4.1 Model simulation parameters

Airflow and dispersion simulations for the first continuous release of IOPs 2, 3, 8, and 9 were performed. The first two of these IOPs occurred during the day, at 1100 Local Time (LT), which was Central Daylight Time. The latter two occurred at night, at 2300 LT. In each case, SF$_6$ was released near the ground as a point source for 30-min, with varying release rates as summarized in Table 1.

For all numerical simulations, a domain size of 1,030 m x 3,010 m x 425 m (in lateral, longitudinal, and vertical directions) was employed. A graded mesh consisting of 201 x 303 x 45 grid points, with a minimal grid spacing of ~1 m near the ground surface, was used. Most of the
buildings within five hundred m of the release point were explicitly resolved and the remaining buildings were treated as virtual buildings. The model domain and building representations appear in Figure 1.

Steady logarithmic velocity profiles provided inflow boundary conditions. These profiles were created based on the 15-minute averaged wind speeds and directions from the PNNL sodar located approximately 2 km SSW of downtown OKC and the hourly averaged data from the weather station on the rooftop of St. Anthony’s hospital at ~1.5 km NW of downtown OKC. The 50m wind speeds and wind direction for these four releases are summarized in Table 1; wind speeds varied from 5-7.2 m/s, while wind directions varied from 155 to 215 degrees. IOP2 was simulated twice, changing the wind direction only. The logarithmic inflow wind profiles appear with the results of the simulations in Figure 2-Figure 5.

For each simulated release, a quasi-steady state flow field was established after ~15 minutes of simulated time prior to the start of the dispersion simulation. The release of SF₆ was modeled as a continuous source over a small area (covered by 2 x 2 cells on the ground surface) at a constant release rate and dispersion results indicate steady state was reached in about 20 minutes of simulated time. For all cases, the RANS approach with the three-equation NEV turbulence parameterization (Gresho and Chan, 1998) was used and neutral atmospheric stability was assumed. Surface-based convection was not imposed because of the lack of appropriate and representative observations to provide boundary conditions. A second run using the LEV turbulence parameterization was also carried out for each IOP, as summarized in Table 1. The LEV parameterization does include the effects of atmospheric stability, but its modeling of mechanically-produced turbulence is less sophisticated than that available in the NEV parameterization, as discussed above.
FEM3MP’s predictions of flow and tracer concentrations in the near and intermediate regions of the release point are presented and compared with observations. For brevity, only major results are presented and compared herein. More detailed model-data comparisons can be found in Chan and Leach (2007) for IOPs 3 and 9. Several of the statistical performance measures recommended by Hanna et al. (1993, 2003) are used to indicate the performance of our model. They are: the fractional bias (FB), the geometric mean bias (MG), the normalized mean square error (NMSE), and the fraction of predictions within a factor of two or five (FAC2 or FAC5).

For weighted differences in angles between predicted and measured wind vectors, the formula of scaled angle differences (SAA) of Calhoun et al. (2004), is used. As summarized in Warner et al. (2004), FB and MG measure the systematic bias of a model in terms of absolute differences and ratios; a perfect model would result in a FB of 0 and a MG of 1. NMSE measures the scatter associated with the predictions relative to observations, and for a perfect model would equal 0, as would SAA. To our knowledge, no community consensus defines acceptable ranges of these metrics.

The equations for these metrics are defined as:

\[
FB = \frac{(C_o - C_p)}{0.5(C_o + C_p)}
\]

\[
MG = \exp\left[\ln\left(\frac{C_o}{C_p}\right)\right]
\]

\[
NMSE = \frac{(C_o - C_p)^2}{C_o C_p}
\]

and

\[
FACx = \text{fraction of data for which } \frac{1}{x} \leq \frac{C_p}{C_o} \leq x,
\]
where $C$ is the observation of interest (e.g., wind speed or tracer concentration), $C_p$ is the model prediction, and $C_o$ is the observation. Overbars denote averages. The SAA, a model performance metric calculated from wind speeds and wind directions, is given by

$$SAA = \frac{\sum_i |U_i||\phi_i|}{N|U_i|},$$

where $\phi_i$ is the angle between predicted and observed velocity vectors and $N$ is the number of samples being averaged. The angle difference is scaled by the magnitude of the predicted velocity vector $|U_i|$ and then is normalized by the average of the magnitudes over all samples. By scaling the angles by the magnitudes, this metric weights the angles of the larger vectors more strongly to minimize the relatively unimportant errors in wind direction associated with small wind speeds.

4.2 Model performance in the near-field

a. Flow field

Airflow in urban areas is extremely complex, with features such as flow separations, local stagnation regions, eddies of various size, and high velocity jets in street canyons. These features were all observed in our model simulations, as documented in Chan and Leach (2007). Visualization of the simulated flow fields are presented in Chan and Leach (2007) for IOPs 3 and 9. For a quantitative model-data comparison of wind vectors at a number of locations for IOPs 2, 3, 8, and 9, we use observations from the twenty DPG PWID sonic anemometers described above, located within the central business district zone. The observed wind speeds and wind directions at these locations for each 30-minute period corresponding to the releases simulated with FEM3MP have been compared with the FEM3MP predictions. These statistical performance measures, based on the twenty PWID datapoints, are summarized in Table 1.
In all cases, the absolute value of the model’s fractional bias (FB) is reasonably good, less than 0.25. A tendency towards over-prediction of wind speeds is seen, with the fractional bias regularly between 0 and -0.25, regardless of whether the sophisticated neutral-stability turbulence parameterization (NEV) or the simpler varying-stability turbulence parameterization (LEV) is utilized. Only for IOP8 is the FB greater than zero. FEM3MP’s systematic over-prediction of winds for these IOPs is also seen in the geometric mean bias (MG), the ratio between model wind speed and observed wind speed. Only for IOP8 is the MG greater than 1. The scatter in the dataset of wind speed observations, as expressed in the NMSE, is small, less than 0.61 (with an average of 0.37 for the NEV simulations). The scaled angle differences are typically less than 30 degrees, and for IOP2, less than 20 degrees. Finally, at least 50% (or 72% on average) of FEM3MP simulated data agree with reported observations within a factor of 2 (FAC2).

Data from two NEV simulations of IOP2 are reported here because of changing wind direction during the simulation period; according to these metrics based on near-field wind flow measurements, the IOP2 simulation with a wind direction of 215 degrees is more consistent with observations based on all the statistical metrics discussed above.

Finally, the flow results using the simpler LEV turbulence parameterization (that accounts for convection) are surprisingly good, often slightly better than the results using the more sophisticated NEV turbulence parameterization (which assumes neutral stability). This subtle improvement in wind field simulation cannot be construed as an endorsement of the LEV turbulence parameterization. As shown below, the NEV turbulence parameterization performs consistently better in predicting the concentration field in all cases, likely because the more
b. Concentration field

The predicted concentration patterns are also compared with observed 15-minute averages of SF6 concentrations from Blue Boxes, of which 10-15 were deployed during each IOP. The locations of the Blue Boxes changed for each IOP, depending on the release location and expectations for vertical transport of SF6. The statistical performance measures of the simulations, compared with the observations, appear in Table 1.

For all IOPs, FEM3MP with the NEV turbulence parameterization could predict the significant upwind and lateral spread of material as indicated by the measured data. The fractional bias metric does indicate a systematic over-prediction of concentrations. One factor contributing to this over-prediction could be the difference between the steady inflow conditions used by the model, as compared to the unsteadiness of the actual winds. This variability would cause a plume to meander, thus reducing the peak values of concentration. Another possible influence could be the averaging time of the data (15 minutes), which is relatively long compared to the duration of the release (30 minutes) and likely does not reflect a “steady-state” result as obtained by the model. Closer inspection of the differences between observed and predicted values indicates no clear pattern to this over-prediction (not shown).

To delineate the stability effects on the dispersion results for these releases, simulations with the LEV parameterization, which includes stability effects but lacks a sophisticated parameterization for building-induced turbulence, were also performed; the resulting metrics for the LEV parameterization also appear in Table 1. Regardless of the metric used to compare observed concentrations with predicted concentrations, the NEV parameterization (which

sophisticated building-induced turbulence parameterization allows for more enhanced plume broadening as well as upwind transport of tracer concentrations.
includes more sophisticated building-induced turbulence) performs much better than the LEV parameterization for both daytime and nighttime releases. These results suggest that building-induced turbulence dominates over any turbulence reduction due to the slightly stable conditions at night or turbulence increase due to convective conditions during the day, thus making the assumption of neutral stability in model simulations justifiable for long-duration releases under moderate wind conditions within a built-up urban area.

4.3 Comparison of simulations with observations in the urban shadow

Wind speed, direction, and turbulence data collected on the crane pseudo-tower (in the urban shadow region, within 1000 km of the downtown area) are analyzed to construct winds and TKE profiles in the area for comparison with the FEM3MP simulations with the NEV turbulence parameterization. These results are considered together to assess the stability conditions associated with these simulations in the urban shadow, as well as to describe the fidelity of the model’s Reynolds-Averaged Navier-Stokes (RANS) simulations to the observed atmosphere.

In Figure 2, a comparison of predicted versus observed profiles of four variables at the crane station for IOP 2 (simulated with an incoming wind direction of 205 degrees) is presented. Included in the comparison are profiles of wind speed, wind direction, friction velocity, and TKE. As is seen in the figure, there is good agreement between the predicted and observed profiles for the wind speed (upper left panel). The FEM3MP simulation slightly under-predicts wind speed compared to all but the top level of the crane, while FEM3MP predicts wind directions that deviate from those measured at the crane by less than 10 degrees.

The friction velocity $u_*$ may be calculated two different ways from the crane data: first, by summing the momentum fluxes at each level independently (the “local” method), as in

$$u_* = \left(\frac{\sqrt{u^2}w^2 + \sqrt{v^2}w^2}{2}\right)^{1/4},$$
and second, by assuming that the profile of wind speeds fit the relationship

$$u_* = \frac{kU}{\ln(z/z_o)},$$

where $k$ is the von Karman constant of 0.4, $U$ is the mean wind speed at each height $z$, and surface roughness $z_o$ is set to 0.5 m in the urban wake to achieve optimal agreement between the local and profile methods. (Note that Gouveia et al. (2007) use a least-squares-fit method based on one month of data from the crane pseudo-tower and find $z_o$ to be at least 0.5 for the wind directions considered here.) Because only this second calculation may be applied to FEM3MP output, only this “profile” method is presented in Figure 2-Figure 5. The simulated estimates of friction velocity are lower than the observed values in the 10-70m levels, as is the case with the wind profiles.

In the lower right panel, the TKE predicted by the model is shown, along with the total TKE observed at the crane site (line with diamond symbols). TKE is directly calculated by the NEV turbulence model in FEM3MP and the data analysis method calculates TKE as

$$\frac{1}{2} (u'^2 + v'^2 + w'^2).$$

Also presented is the TKE profile with an estimate of the buoyant production contribution removed, against which the predicted profile should be compared. The two observed TKE profiles suggest that buoyant production contributes only between 5% and 25% of the total TKE budget for this IOP, one of the two daytime IOPs in which buoyant forcing is expected to be a significant contributor to the total turbulence budget.

In the lower right panel of Figure 3, a similar profile of simulated, observed, and observed minus buoyant TKE is presented for IOP3. For this case, the shapes of the TKE profiles are quite similar, though the model underpredicts the amount of TKE observed at the actual crane site. The estimate of buoyant contribution to the total observed TKE is much smaller for this daytime
IOP, less than 10% at maximum. The crane observations do indicate higher wind speeds at the highest levels of the crane for IOP3 than for IOP2, thus suggesting increased shear and therefore increased mechanical production of turbulence in the CBD area. As in the case of IOP2, the simulations underpredict wind speed and friction velocity at the crane location. The wind direction profile indicates that the simulation wind direction was likely off by 5-10 degrees. With the shift in wind direction and the observations that buoyant production of turbulence is an order of magnitude smaller than shear production of turbulence, we assume that the omission of buoyancy effects in the NEV turbulence parameterization is not responsible for the deviations from the observations.

The two daytime IOPs are expected to depict the strongest role of buoyant forcing, while nighttime IOPs are expected to be more classically neutral. In Figure 4, a comparison of predicted versus observed profiles of wind speed, wind direction, friction velocity, and TKE, at the crane pseudo-tower for nocturnal IOP 8 is presented. Although the simulation again underpredicts wind speed, friction velocity, and TKE, the shapes of the profiles are generally consistent with observations. Model predictions for both wind speed and friction velocity at the crane top are only approximately 65% of the observed values. The discrepancies between observations and simulations for IOP 8 could be due to larger scale flow processes not currently accounted for in our simulation, particularly the vertical transport of momentum and turbulence. Lundquist and Mirocha (2006, 2007) discuss the occurrence of a nocturnal low-level jet on the night of IOP 8 based on data from the pseudo-tower and the PNNL boundary-layer wind profiler 2 km SSW of the OKC urban core. Shear generated by the low-level jet (seen in Figure 15 of Lundquist and Mirocha (2006)) could be responsible for the vertical transport of momentum from upper levels into the lower levels simulated here, thereby increasing wind speed, friction
velocity, and TKE. Because this present simulation excludes the possibility of vertical transport of momentum from outside the simulation domain, such processes are not simulated here, and therefore could explain some of the discrepancies between observations and simulations.

In the upper right panel, the predicted and observed profiles for the wind direction are compared. The agreement between predicted and observed profiles is generally good except for $z=15$ to $30$ m, with the largest under-prediction of the angle by $\sim10^\circ$ near $z=15$ m AGL. In the lower right panel, profiles of observed TKE, observed TKE without buoyant production, and predicted TKE are displayed. The two observed TKE profiles suggest that buoyant production, in this case, is negligible. Also, as seen in Table 2, observations indicate the rate of buoyant production of turbulence is two orders of magnitude smaller than shear production of turbulence. (And observations show buoyant production of turbulence rather than suppression.) The predicted and observed profiles have similar shapes, although the predicted values are only about 55% of those observed. Again, the possibility of a nocturnal jet present during the release is a plausible explanation for the higher TKE observed. Most importantly in the context of the present study, buoyant forcing plays no consequential role, either in production or suppression of turbulence in the crane observations, underscoring the suitability of an assumption of neutral stability for urban nocturnal simulations of long-duration releases.

Finally, Figure 5 compares predicted and observed profiles for IOP 9. The wind speeds, as predicted by the model, are slight overpredictions compared to observations, while the wind direction is as much as 20 degrees away from observed wind directions. Profiles of friction velocity are slightly greater than observed, which is consistent with the slightly elevated wind speeds observed. The TKE profiles predicted by the model agree quite well with those observed at the crane location. As with IOP8, the role of buoyancy is minimal during this nocturnal
release, with buoyant effects creating a small amount of turbulence, an order of magnitude less than shear effects. The simulation of this IOP agrees well with the observations, perhaps due to the fact that, as discussed in Lundquist and Mirocha (2006, 2007), no vertical transport of momentum from outside the simulation domain affects the flow.

4.4 Observed TKE budgets in the urban shadow

TKE budgets are estimated from the crane pseudo-tower data, with dissipation, shear production, buoyant production or destruction, and turbulent transport calculated directly. The residual term includes advected turbulence, pressure transport, and the accumulated errors from the directly calculated terms. The TKE budgets corresponding to the releases simulated from IOPs 2, 3, 8, and 9 appear in Figure 6, presented dimensionally. The largest directly-calculated term for all IOPs is the dissipation term, which is consistent with expectations for a site immediately downwind of a large source of TKE production. Values for dissipation rate range from 0.004 m$^2$s$^{-3}$ to 0.09 m$^2$s$^{-3}$, well within the range observed in disturbed boundary layers (Piper and Lundquist, 2004). Shear production tends to be the next largest term, although for IOP3, turbulent transport is very large at the lower levels of the crane. Finally, buoyant production or destruction of TKE is small even for the daytime IOPs (IOP 2 and IOP 3), which implies that buoyant forcing is not a critical consideration for simulations of long-duration releases in the shadow of an urban area. The storage of TKE is one to two orders of magnitude smaller than the shear production term.

The shapes of the budget profiles merits comment. For all IOPs, shear production increases with height, as expected for canopy flows. Dissipation rates are higher near the surface than aloft for the daytime IOPs, which exhibit moderate average wind speeds and flow from the south-south-west. For the nighttime IOPs, with lighter average wind speeds and flow from the south-
south-east, dissipation rates increase with height. For all IOPs, the turbulent transport of TKE tends to peak around 30m, which is approximately the average height of buildings in the downtown area. The residual term, which includes the advection term as well as any pressure transport and the accumulated errors of the directly-calculated terms, mirrors largely the dissipation term. Because of the large dissipative term, we hypothesize, in view of the average TKE values discussed in the next sub-section, that most of the observed TKE is generated within the urban matrix and advected downwind to be dissipated rather than advected in from outside the computational domain. A complete test of that hypothesis would require two sets of similar observations, both upwind and far downwind of the urban domain, and we encourage future field experiments to deploy such instrumentation if possible.

For each IOP, the portion of TKE due to buoyancy effects is estimated by multiplying the buoyant production rate $B$ by a turbulent time scale $\tau$, which is given by the total TKE over the dissipation rate $\varepsilon$. Values averaged over all crane levels for each IOP are summarized in Table 2. The turbulent time scales are all short, between one and two minutes, likely because of the small size of turbulent eddies at the crane pseudo-tower just downwind of the central business district in the urban shadow. (Recall that for convective boundary layers over homogeneous fetch, a turbulent time scale is typically calculated to be on the order of 10-20 minutes, for a boundary layer 1-2 km deep with convective eddies rising at 1-2 m s$^{-1}$.) The consistency between estimates of the turbulent time scale, for different IOPs does suggest the possibility of coherent structures downwind of the urban area. In summary, only for IOP2, which had a lower wind speed than the other daytime IOP, does portion of TKE due to buoyant forcing become significant. At this location in the urban shadow, the rate of buoyant production of turbulence is always at least an order of magnitude smaller than the shear production of turbulence. It is also
interesting to note that in all IOPs buoyancy effects are always observed to produce turbulence, rather than suppress it, even during the nighttime IOPs.

4.5 Variability of TKE in the upwind – urban – urban shadow – downwind wake regions

As argued above, neutral stability is often presumed in urban areas due to the enhanced mechanical mixing found in complexes of building geometries. In all of these simulations, significant TKE due to building-induced turbulence was generated. Due to the generation of strong turbulent shear stresses as a result of the flow impinging on building walls and flow separation from building edges, regions with the highest turbulence intensity are generally on the edges of the CBD in close alignment with the streamwise direction, as seen in Figure 7, which depicts TKE contours at 32m above the surface (average building height) for all four IOPs, focusing on the central business district. The regions of highest turbulence intensity coincide with regions of large horizontal shear, and so most of the TKE production in these regions can therefore be attributed to shear production.

Averaged TKE, integrated across the computational domain and for the lowest 200m, offers insight into the generation and decay of mechanically-produced TKE. These integrated values are presented in Figure 8 as a function of north-south distance for all IOPs, which loosely approximates distance upwind and downwind. For comparison purposes four zones may be defined, somewhat arbitrarily. The zones are defined as: upwind (y=-400 m to 0, in Figure 1), urban CBD (y=200 m to 1000 m), downwind urban shadow (y=1000m to 2000m) and downwind wake (y=2000 m to 2600 m). (The location of the crane observing tower, used above, is at y = 1200m, within the urban shadow region.) Note that only the urban CBD zone appears in its entirety in Figure 7. The same crosswind extent of 900m, centered on the intersection of Reno and Robinson, and the same vertical extent, from the surface to 200m, are used in all four zones.
The averaged TKE values are presented in Table 3 and appear in Figure 8 as horizontal dotted lines. The crane pseudo-tower is located within the urban shadow; values observed at that location also appear in Figure 8 as asterisks. Substantial deviation between the crane observation at one location and the average across the east-west band is expected.

These values indicate a significant increase in turbulence intensity due to increased shear production of TKE in the urban CBD zone for all IOPs. The turbulence intensity in the urban area is at least five times that at upwind and is about three times (with the exception of a value of 1.6 for IOP9, which will be discussed later) that in the urban wake. The urban shadow region, or the transition between the CBD and the downtown urban wake region, exhibits an exponential decay of turbulence which seems to be a function of wind speed, and so mean values are not particularly descriptive for this region in which turbulence generated within the CBD dissipates as it is advected downwind. Due to turbulence transport from the urban area, turbulence intensity in the far downwind wake area is slightly higher than that in the upwind region. Assuming the averaged TKE value at upwind is representative of the turbulence level in the rural area, the above estimates suggest that building-induced mechanical stresses have caused the turbulence intensity to increase by as much as seven times in the urban area. The two sets of values (for IOP 2) also indicate the incoming wind flow direction is not a strong factor in determining the averaged TKE values in different zones, at least for the slightly varying wind directions considered herein for Oklahoma City.

The ratio between CBD turbulence and turbulence in the urban wake exhibits a slight trend with incoming wind speed: IOP9, with the highest incoming wind speed of 7.2 m/s, has the lowest ratio of CBD to wake turbulence. Because CBD-generated turbulence is advected downwind faster in this simulation, as compared with the other simulations, it is conceivable that
less dissipation of CBD turbulence has taken place by the time that turbulence enters the “urban wake” zone.

The information in Figure 8, particularly the length of the urban shadow exponential decay, could be used to indicate the regions in which neutral stability may be assumed appropriately. However, this calculation is highly dependent on wind speed and somewhat on wind direction, and should therefore be pursued in the context of creating a reference for locations of interest rather than general guidelines for all urban areas. The nature of the curves in Figure 8 are indicative of turbulence generated in Oklahoma City and may not be representative of other locations, especially those with different urban geometries.

5. Conclusions

In this paper, the validity of omitting stability considerations when simulating long-duration transport and dispersion in the urban environment is explored using observations from the Oklahoma City Joint URBAN 2003 field experiment and computations fluid dynamics simulations of that experiment. Four IOPs, two daytime (IOP2 and IOP3) and two nighttime (IOP8 and IOP9), have been simulated using the building-resolving FEM3MP computational fluid dynamics model to solve the Reynolds Averaged Navier-Stokes equations using two possible turbulence parameterizations and a mixed virtual-explicit building representation. Model performance metrics are calculated for the downtown area based on wind fields and tracer concentrations; in the urban shadow, model wind and turbulence fields are compared with observed profiles. Model predictions for all four IOPs, regarding winds, concentrations, profiles of wind speed, wind direction, and friction velocity, are generally consistent with and compare reasonably well with the field observations. Simulations using the NEV turbulence parameterization, which omits stability considerations but includes complex building-induced
turbulence production, generally agree better with observations than simulations that do account for stability at the expense of a less-complex mechanical turbulence model, although neither set of simulations accounts for forced convection. The shapes of the predicted TKE profiles are similar to those observed in the urban shadow for all cases. However, the predicted turbulence intensities are in general too low, except for the case of IOP9, for which wind speeds were somewhat overpredicted as well.

Inspection of the observations, including the TKE budget as measured at the crane pseudo-tower in the urban shadow, indicate a minimal role of buoyant forcing. The largest term of the TKE budget is the dissipation rate, which is balanced by a residual term which includes the advection of turbulence from upwind as well as pressure transport of TKE and errors in other calculations. Considering the large urban matrix found upwind of the observing station, and that significant turbulence is expected to be generated by flow through that area, we assume that much of the residual is attributable to advection of TKE from the downtown CBD. The buoyant production of TKE is always found to be positive, even at night, but typically found to be an order of magnitude or more less than the shear production of TKE. We conclude that buoyancy plays a minimal role in the production of TKE even in the urban shadow. The FEM3MP simulations’ deviations from the observations therefore do not seem to be related to “missing” buoyant forcing due to the assumption of neutral stability in the NEV turbulence parameterization. These deviations are most likely due to other sources including inaccuracies in boundary conditions (e.g., inflow conditions), inadequate representation of large-scale forcing (e.g. low-level jets, in the case of IOP 8), and to a lesser extent the possible limitations of the turbulence parameterizations used in this study.
Turbulent timescales are calculated to quantify further the importance of buoyant forcing relative to the total TKE. For IOP 2 (a daytime release with low wind speeds), the buoyancy production contributes no more than 25% to the total TKE budget in the region. Buoyancy plays less of a role in the other daytime release, IOP 3, probably due to the stronger winds in that case and the increased role of mechanical forcing. For both IOP 8 and IOP 9, nighttime releases, the contribution of buoyancy production to the total TKE budget in the same region is negligible.

Estimates of the average TKE values in various zones of the computational domain suggest that building-induced turbulence can cause the average turbulence intensity in the urban area to increase by as much as seven times typical upwind values. This increase persists in the urban shadow but decays exponentially, relaxing by approximately 1 kilometer downwind. In a wake region defined to be 1.5 km downwind and beyond, simulations show most of the urban-produced TKE has decayed. The exact downwind distance required for decay seems to be a function of wind speed for two reasons. First, higher wind speeds involve more shear and more production of turbulence, and second, higher wind speeds advect turbulence downwind faster. The dissipation of a given amount of TKE would require more distance to occur in a case with higher wind speed. Average TKE values in the upwind, downtown, and urban wake regions appear independent of the wind directions considered in this study.

Considering that buoyancy effects are negligible during the nighttime releases (IOP 8 and IOP 9), the assumption of neutral stability for nighttime simulations in the downtown and downtown shadow is acceptable. For one daytime release (IOP 2), although the buoyancy production could contribute up to 25% of the TKE budget, the assumption of neutral stability in the downtown and downtown shadow is still valid because building-induced turbulence is the dominant source of TKE in the area. Due to higher wind speeds in the other daytime release (IOP
3), buoyancy effects are minimal and can be neglected. However, in areas approximately 1.5 km and further downwind, the levels of building-induced turbulence subside rapidly. Therefore, in these downwind regions, the assumption of neutral stability is less valid. Considering that building-induced mechanical turbulence plays a subdued role in these regions, it is likely that buoyancy effects should be considered in flow and dispersion simulations for those regions, at least for cities like Oklahoma City with concentrated central urban areas.

These conclusions are based on RANS simulations and relatively long releases (30 min) of tracer gas, which average out the effects of localized buoyant plumes and differential heating. Those localized buoyant effects, which were observed even at night in Oklahoma City, could become consequential for shorter-duration or “instantaneous” releases even within the downtown area.

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References


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*AIAA Journal, **24**, 1606-1610.*
List of Captions

Figure 1: The central business district (CBD) of OKC as represented in the FEM3MP model domain. Explicitly-resolved buildings appear in black with sharp edges. Grayscale indicates the height of virtually-resolved buildings. Note that some virtual buildings may be taller than the 30m maximum shown here. All explicitly-resolved buildings are south of y=700, north of y=0, and east of x=-200 and west of x=200.

Figure 2: Comparison of predicted versus observed profiles at crane station for IOP2: wind speed (upper left), wind direction (upper right), friction velocity (lower left), and TKE (lower right).

Figure 3: As in Figure 2 but for IOP3.

Figure 4: As in Figure 2 but for IOP8.

Figure 5: As in Figure 2 but for IOP9.

Figure 6: Profiles of the turbulence kinetic energy budget as measured at the crane pseudo-tower for IOPs 2 (top left), 3 (top right), 8 (bottom left), and 9 (bottom right). The mean wind speed and wind direction during the first continuous release of each IOP is noted in the title of each figure. For all IOPs, the dissipation rate is very large. The residual term, also large for all IOPs, consists of advected turbulence, the pressure transport of turbulence, and accumulated errors from the estimation of the other terms.
Figure 7: Contours of TKE for all four IOPs as simulated by FEM3MP with the NEV turbulence parameterization and mixed virtual-explicit buildings. Only the explicitly-resolved buildings appear, denoted with darkest shading. Units of the TKE contours are m2s-2.

Figure 8: Averaged TKE in the computational domain for all IOPs, integrated from -450 < x < 450 m, 10 < z < 200 m, with distances corresponding to those shown in Figure 1. IOP2, top right, shows results from two simulations: solid line shows inflow wind direction of 205 degrees, dashed line shows inflow wind direction of 215 degrees. The dotted horizontal lines indicate the average TKE for the upwind (-400 < y< 0), CBD (200<y<1000), urban shadow (1000<y<2000), and urban wake (2000<y<2600m) zones. Asterisks located at y=1200 indicate average TKE values from the crane pseudo-tower location.
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Table 1: Summary of FEM3MP simulations and statistics discussed herein

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**FLOW STATISTICS**

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**DISPERSION STATISTICS**

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Table 2: Observations at the crane of mean TKE and mean dissipation rate used to calculate a mean turbulent time scale. Mean rate of buoyant production of TKE is also shown; the products of the time scale and buoyant production rate are used to estimate the portion of TKE due to buoyant production.

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<th>IOP</th>
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<th>Mean dissipation rate (m$^2$ s$^{-3}$)</th>
<th>Mean turbulent time scale (sec)</th>
<th>Mean buoyant production rate (m$^2$ s$^{-3}$)</th>
<th>Mean shear production rate (m$^2$ s$^{-3}$)</th>
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<td>7.06 x 10^{-3}</td>
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Table 3: Average TKE in the upwind, CBD, urban shadow, and urban wake zones for five FEM3MP simulations. Note that the urban shadow region is characterized by an exponential decay of TKE with distance from the CBD rather than the mean value listed here.

<table>
<thead>
<tr>
<th></th>
<th>IOP2</th>
<th>IOP3</th>
<th>IOP8</th>
<th>IOP9</th>
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<tr>
<td>50m wind speed (m/s)</td>
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<td>50m wind direction (deg)</td>
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<td>CBD/Wake TKE</td>
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